

Nature of the Excited States of the Even-Even $^{98-108}\text{Ru}$ Isotopes

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The positive and negative parity states of the even-even $^{98-108}\text{Ru}$ isotopes are studied within the frame work of the interacting boson approximation model ($IBA-1$). The calculated levels energy, potential energy surfaces, $V(\beta, \gamma)$, and the electromagnetic transition probabilities, $B(E1)$ and $B(E2)$, show that ruthenium isotopes are transitional nuclei. Staggering effect, $\Delta I = 1$, has been observed between the positive and negative parity states in some of ruthenium isotopes. The electric monopole strength, $X(E0/E2)$, has been calculated. All calculated values are compared with the available experimental and theoretical data where reasonable agreement has been obtained.

1 Introduction

The mass region $A = 100$ has been of considerable interest for nuclear structure studies as it shows many interesting features. These nuclei show back bending at high spin and shape transitions from vibrational to γ -soft and rotational characters. Many attempts have been made to explore these structural changes which are due mainly to the n-p interactions.

Experimentally, the nuclear reaction $^{100}\text{Mo}(\alpha, xn)$ [1] has been used in studying levels energy of ^{100}Ru . Angular distribution, γ - γ coincidences were measured, half life time has been calculated and changes to the level scheme were proposed. Also, double beta decay rate of ^{100}Mo to the first excited 0^+ state of ^{100}Ru has been measured experimentally [2] using γ - γ coincidence technique.

Doppler-shift attenuation measurements following the $^{100}\text{Ru}(n, n'\gamma)$ reaction [3] has been used to measure the life times of the excited states in ^{100}Ru . Absolute transition rates were extracted and compared with the interacting boson model description. The $2^+(2240.8 \text{ keV})$ state which decays dominantly to the 2^+ via 1701 keV transition which is almost pure $M1$ in nature considered as a mixed-symmetry state. Again ^{100}Ru has been studied [4] experimentally and several levels were seen where some new ones are detected below 3.2 MeV.

The excited states of ^{102}Ru have been investigated using $^{96}\text{Zr}(^{10}\text{B}, p3n)$ reaction [5] at a beam of energy 42 MeV and the emitted γ rays were detected. The analysis indicated that the nucleus is a γ -soft and the band crossing as well as staggering effect have been observed.

Theoretically many models have been applied to ruthenium isotopes. Yukawa folded mean field [6] has been applied to ^{100}Ru nucleus while the microscopic vibrational model has been applied to ^{104}Ru and some other nuclei with their daughters [7]. The latter model was successful in describing the yrast 0^+ and 2^+ states of most of these nuclei and also some of their half-lives.

The very high-spin states of nuclei near $A \approx 100$ are inves-

tigated by the Cranked Strutinsky method [8] and many very extended shape minima are found in this region. Interacting boson model has been used in studying Ru isotopes using a $U(5)-O(6)$ transitional Hamiltonian with fixed parameters [9, 10] except for the boson number N . The potential arising from a coherent-state analysis indicates that ^{104}Ru is close to the critical point between spherical and γ -unstable structures.

Hartree-Fock Bogoliubov [11] wave functions have been tested by comparing the theoretically calculated results for ^{100}Mo and ^{100}Ru nuclei with the available experimental data. The yrast spectra, reduced $B(E2, 0^+ \rightarrow 2^+)$ transition probabilities, quadrupole moments $Q(2^+)$ and g factors, $g(2^+)$ are computed. A reasonable agreement between the calculated and observed has been obtained.

The microscopic anharmonic vibrator approach (MAVA) [12] has been used in investigating the low-lying collective states in $^{98-108}\text{Ru}$. Analysis for the level energies and electric quadrupole decays of the two-phonon type of states indicated that ^{100}Ru can be interpreted as being a transitional nucleus between the spherical anharmonic vibrator ^{98}Ru and the quasirotational $^{102-106}\text{Ru}$ isotopes.

A new empirical approach has been proposed [13] which is based on the connection between transition energies and spin. It allows one to distinguish vibrational from rotational characters in atomic nuclei. The cranked interacting boson model [14] has been used in estimating critical frequencies for the rotation-induced spherical-to-deformed shape transition in $A = 100$ nuclei. The predictions show an agreement with the back bending frequencies deduced from experimental yrast sequences in these nuclei.

The aim of the present work is to use the $IBA-1$ [15-17] for the following tasks:

- (1) calculating the potential energy surfaces, $V(\beta, \gamma)$, to know the type of deformation exists;
- (2) calculating levels energy, electromagnetic transition rates $B(E1)$ and $B(E2)$;

nucleus	<i>EPS</i>	<i>PAIR</i>	<i>ELL</i>	<i>QQ</i>	<i>OCT</i>	<i>HEX</i>	<i>E2SD(eb)</i>	<i>E2DD(eb)</i>
⁹⁸ Ru	0.6280	0.000	0.0090	-0.0010	0.0000	0.0000	0.1250	-0.3698
¹⁰⁰ Ru	0.5950	0.000	0.0085	-0.0200	0.0000	0.0000	0.1160	-0.3431
¹⁰² Ru	0.5650	0.0000	0.0085	-0.0200	0.0000	0.0000	0.1185	-0.3505
¹⁰⁴ Ru	0.4830	0.0000	0.0085	-0.0200	0.0000	0.0000	0.1195	-0.3535
¹⁰⁶ Ru	0.4560	0.0000	0.0085	-0.0200	0.0000	0.0000	0.1020	-0.3017
¹⁰⁸ Ru	0.4540	0.0000	0.0085	-0.0200	0.0000	0.0000	0.1035	-0.3062

Table 1: Parameters used in IBA-1 Hamiltonian (all in MeV).

- (3) studying the relation between the angular momentum I , the rotational angular frequency $\hbar\omega$ for bending in ruthenium isotopes;
- (4) calculating staggering effect and beat patterns to detect any interactions between the (+ve) and (-ve) parity states; and
- (5) calculating the electric monopole strength $X(E0/E2)$.

2 (IBA-1) model

2.1 Level energies

IBA-1 model was applied to the positive and negative parity states in even-even ⁹⁸⁻¹⁰⁸Ru isotopes. The Hamiltonian employed in the present calculation is:

$$\begin{aligned}
 H = & EPS \cdot n_d + PAIR \cdot (P \cdot P) \\
 & + \frac{1}{2} ELL \cdot (L \cdot L) + \frac{1}{2} QQ \cdot (Q \cdot Q) \\
 & + 5OCT \cdot (T_3 \cdot T_3) + 5HEX \cdot (T_4 \cdot T_4),
 \end{aligned} \quad (1)$$

where

$$P \cdot P = \frac{1}{2} \left[\begin{array}{c} \left\{ (s^\dagger s^\dagger)_0^{(0)} - \sqrt{5} (d^\dagger d^\dagger)_0^{(0)} \right\} x \\ \left\{ (ss)_0^{(0)} - \sqrt{5} (\tilde{d}\tilde{d})_0^{(0)} \right\} \end{array} \right]_0^{(0)}, \quad (2)$$

$$L \cdot L = -10 \sqrt{3} \left[(d^\dagger \tilde{d})^{(1)} x (d^\dagger \tilde{d})^{(1)} \right]_0^{(0)}, \quad (3)$$

$$Q \cdot Q = \sqrt{5} \left[\begin{array}{c} \left\{ (S^\dagger \tilde{d} + d^\dagger s)^{(2)} - \frac{\sqrt{7}}{2} (d^\dagger \tilde{d})^{(2)} \right\} x \\ \left\{ (s^\dagger \tilde{d} + \tilde{d}s)^{(2)} - \frac{\sqrt{7}}{2} (d^\dagger \tilde{d})^{(2)} \right\} \end{array} \right]_0^{(0)}, \quad (4)$$

$$T_3 \cdot T_3 = -\sqrt{7} \left[(d^\dagger \tilde{d})^{(2)} x (d^\dagger \tilde{d})^{(2)} \right]_0^{(0)}, \quad (5)$$

$$T_4 \cdot T_4 = 3 \left[(d^\dagger \tilde{d})^{(4)} x (d^\dagger \tilde{d})^{(4)} \right]_0^{(0)}. \quad (6)$$

In the previous formulas, n_d is the number of boson; $P \cdot P$, $L \cdot L$, $Q \cdot Q$, $T_3 \cdot T_3$ and $T_4 \cdot T_4$ represent pairing, angular momentum, quadrupole, octupole and hexadecupole interactions

between the bosons; *EPS* is the boson energy; and *PAIR*, *ELL*, *QQ*, *OCT*, *HEX* is the strengths of the pairing, angular momentum, quadrupole, octupole and hexadecupole interactions.

2.2 Transition rates

The electric quadrupole transition operator employed in this study is:

$$\begin{aligned}
 T^{(E2)} = & E2SD \cdot (s^\dagger \tilde{d} + d^\dagger s)^{(2)} + \\
 & + \frac{1}{\sqrt{5}} E2DD \cdot (d^\dagger \tilde{d})^{(2)}.
 \end{aligned} \quad (7)$$

The reduced electric quadrupole transition rates between $I_i \rightarrow I_f$ states are given by

$$B(E2, I_i \rightarrow I_f) = \frac{[< I_f || T^{(E2)} || I_i >]^2}{2I_i + 1}. \quad (8)$$

3 Results and discussion

3.1 The potential energy surfaces

The potential energy surfaces [18], $V(\beta, \gamma)$, as a function of the deformation parameters β and γ are calculated using:

$$\begin{aligned}
 E_{N_\pi N_\nu}(\beta, \gamma) = & < N_\pi N_\nu; \beta \gamma | H_{\pi\nu} | N_\pi N_\nu; \beta \gamma > = \\
 = & \zeta_d(N_\nu N_\pi) \beta^2 (1 + \beta^2) + \beta^2 (1 + \beta^2)^{-2} \times \\
 & \times \{ k N_\nu N_\pi [4 - (\bar{X}_\pi \bar{X}_\nu) \beta \cos 3\gamma] \} + \\
 & + \left\{ [\bar{X}_\pi \bar{X}_\nu \beta^2] + N_\nu (N_\nu - 1) \left(\frac{1}{10} c_0 + \frac{1}{7} c_2 \right) \beta^2 \right\},
 \end{aligned} \quad (9)$$

where

$$\bar{X}_\rho = \left(\frac{2}{7} \right)^{0.5} X_\rho \quad \rho = \pi \text{ or } \nu. \quad (10)$$

The calculated potential energy surfaces, $V(\beta, \gamma)$, are presented in Fig. 1. It shows that ⁹⁸Ru is a vibrational — like nucleus while ¹⁰⁰⁻¹⁰⁴Ru are γ -soft where the two wells on the oblate and prolate sides are equal. ^{106,108}Ru are rotational - like where they are prolate deformed.

$I_i^+ I_f^+$	^{98}Ru	^{100}Ru	^{102}Ru	^{104}Ru	^{106}Ru	^{108}Ru
$0_1 \text{ Exp}^*. 2_1$	0.392(12)	0.490(5)	0.630(10)	0.820(12)	0.770(20)	1.010(15)
$0_1 \text{ Theor. } 2_1$	0.3930	0.4853	0.6279	0.8274	0.7737	1.0110
$2_1 0_1$	0.0786	0.0970	0.1256	0.1655	0.1547	0.2022
$2_2 0_1$	0.0000	0.0006	0.0012	0.0027	0.0032	0.0040
$2_2 0_2$	0.0226	0.0405	0.0548	0.0826	0.0870	0.1257
$2_3 0_1$	0.0000	0.0000	0.0000	0.0002	0.0006	0.0017
$2_3 0_2$	0.0658	0.0759	0.0993	0.1135	0.0853	0.0830
$2_3 0_3$	0.0093	0.0087	0.0121	0.0207	0.0264	0.0402
$2_4 0_3$	0.0041	0.0066	0.0121	0.0286	0.0448	0.0795
$2_4 0_4$	0.0565	0.0588	0.0712	0.0786	0.0530	0.0448
$4_1 2_1$	0.1260	0.1683	0.2257	0.3071	0.2912	0.3791
$4_1 2_2$	0.0092	0.0142	0.0190	0.0271	0.0267	0.0360
$4_1 2_3$	0.0269	0.0319	0.0424	0.0498	0.0384	0.0386
$6_1 4_1$	0.1420	0.2039	0.2838	0.3897	0.3681	0.4747
$6_1 4_2$	0.0172	0.0179	0.0228	0.0285	0.0256	0.0323
$6_1 4_3$	0.0208	0.0242	0.0333	0.0382	0.0292	0.0300
$8_1 6_1$	0.1264	0.2032	0.2998	0.4208	0.4012	0.5194
$8_1 6_2$	0.0247	0.0183	0.0223	0.0256	0.0217	0.0265
$8_1 6_3$	0.0113	0.0157	0.0239	0.0286	0.0228	0.0247
$10_1 8_1$	0.0791	0.1678	0.2768	0.4081	0.3997	0.5264
$10_1 8_2$	0.0319	0.0175	0.0207	0.0224	0.0183	0.0217

*Ref. 19.

Table 2: Values of the theoretical reduced transition probability, $B(E2)$ (in $e^2 b^2$).

$I_i^+ I_f^+$	^{98}Ru	^{100}Ru	^{102}Ru	^{104}Ru	^{106}Ru	^{108}Ru
$1_1 0_1$	0.0000	0.0030	0.0050	0.0104	0.0176	0.0261
$1_1 0_2$	0.1084	0.1280	0.1285	0.1280	0.1258	0.1227
$3_1 2_1$	0.1055	0.1211	0.1219	0.1306	0.1432	0.1564
$3_1 2_2$	0.0470	0.0415	0.0471	0.0544	0.0618	0.0712
$3_1 2_3$	0.0013	0.0002	0.0000	—	0.7737	—
$3_2 2_1$	0.0158	0.0024	0.0018	0.0029	0.0067	0.0130
$3_2 2_2$	0.0347	0.0197	0.0136	0.0102	0.0104	0.0121
$3_2 2_3$	0.1600	0.2126	0.2119	0.1943	0.1660	0.1352
$5_1 4_1$	0.2261	0.2533	0.2533	0.2605	0.2737	0.2881
$5_1 4_2$	0.0608	0.0480	0.0563	0.0648	0.0714	0.0784
$5_1 4_3$	0.0020	0.0006	—	—	0.7737	—
$7_1 6_1$	0.3657	0.3950	0.3912	0.3970	0.4083	0.4213
$7_1 6_2$	0.0609	0.0446	0.0551	0.0641	0.0701	0.0757
$9_1 8_1$	0.5276	0.5439	0.5367	0.5386	0.5465	0.5568
$9_1 8_2$	0.0425	0.0342	0.0472	0.0574	0.0640	0.0695
$11_1 10_1$	0.7143	0.6983	0.6872	0.6845	0.6882	0.6951

Table 3: Values of the theoretical reduced transition probability, $B(E1)$ (in $\mu e^2 b$).

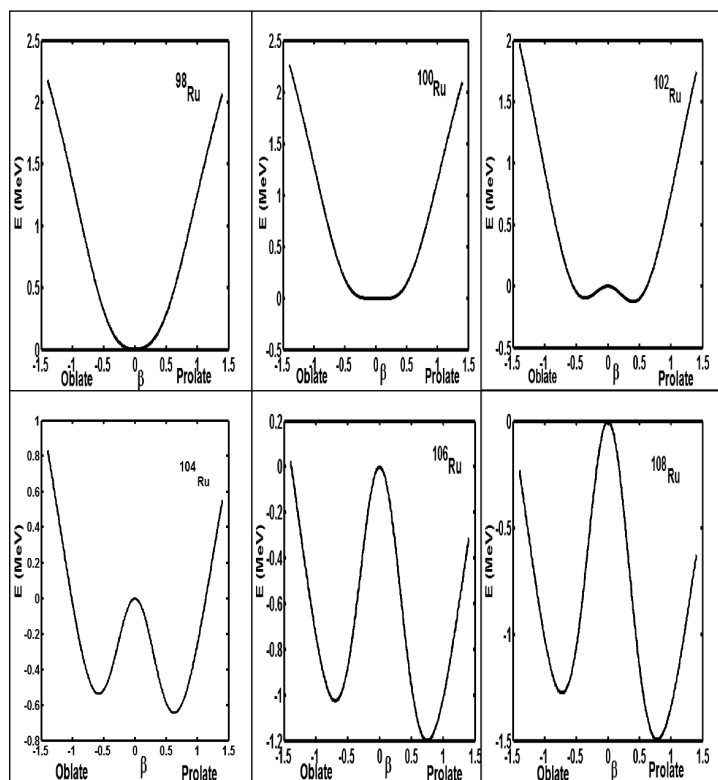
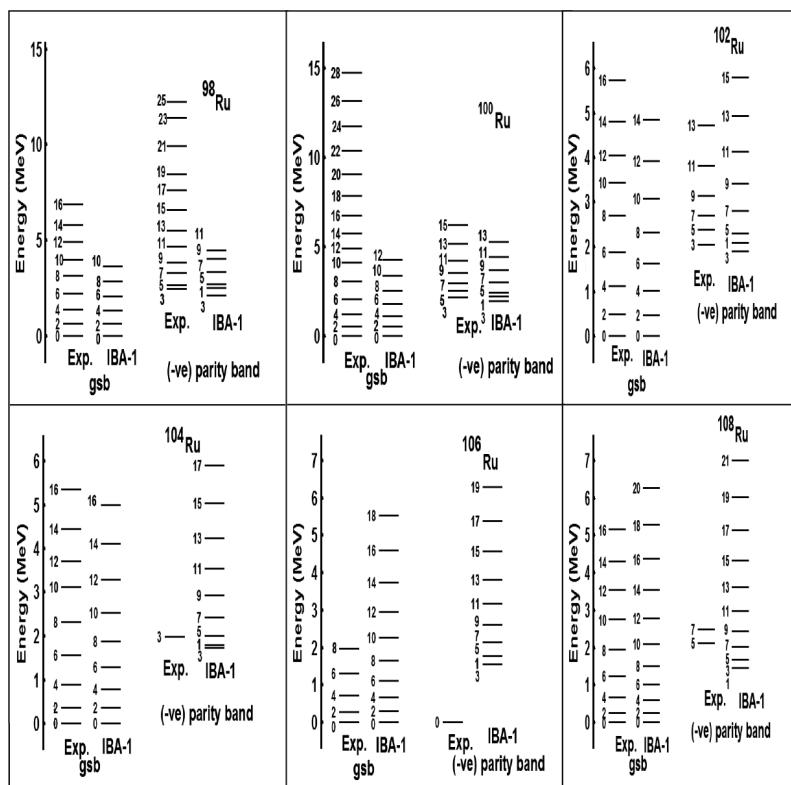
Fig. 1: Potential energy surfaces for $^{98-108}\text{Ru}$ nuclei.

Fig. 2: Comparison between exp. [21–26] and theoretical (IBA-1) energy levels.

I_i^+	I_f^+	I_{if}^+	^{98}Ru	^{100}Ru	^{102}Ru	^{104}Ru	^{106}Ru	^{108}Ru
0 ₂	0 ₁	2 ₁	0.011	0.027	0.057	0.166	0.213	0.227
0 ₃	0 ₁	2 ₁	0.250	0.347	1.333	0.894	1.076	1.328
0 ₃	0 ₁	2 ₂	0.001	0.009	0.005	0.010	0.086	0.112
0 ₃	0 ₁	2 ₃	1.000	0.042	0.026	0.024	0.043	0.130
0 ₃	0 ₂	2 ₁	—	0.086	0.500	0.421	0.184	0.171
0 ₃	0 ₂	2 ₂	—	0.002	0.002	0.004	0.014	0.014
0 ₃	0 ₂	2 ₃	—	0.010	0.010	0.011	0.007	0.016
0 ₄	0 ₁	2 ₂	1.600	0.010	0.046	—	—	—
0 ₄	0 ₁	2 ₃	0.024	0.010	0.003	—	—	—
0 ₄	0 ₁	2 ₄	0.363	0.113	0.003	—	—	—
0 ₄	0 ₂	2 ₂	1.200	0.030	0.097	—	—	—
0 ₄	0 ₂	2 ₃	0.018	0.034	0.070	0.114	0.476	0.808
0 ₄	0 ₂	2 ₄	0.272	0.340	0.142	1.035	3.696	2.082
0 ₄	0 ₃	2 ₁	0.111	0.454	—	—	0.558	0.458
0 ₄	0 ₃	2 ₂	0.600	0.010	0.010	—	0.002	0.611
0 ₄	0 ₃	2 ₃	0.009	0.011	0.007	—	0.074	0.058
0 ₄	0 ₃	2 ₄	0.136	0.113	0.015	—	0.575	0.150

Table 4. Theoretical $X_{if} (E0/E2)$ in Ru isotopes.

3.2 Energy spectra

The energy of the positive and negative parity states of ruthenium series of isotopes are calculated using computer code PHINT [20]. A comparison between the experimental spectra [21–26] and our calculations, using values of the model parameters given in Table 1 for the ground state band are illustrated in Fig. 2. The agreement between the calculated levels energy and their correspondence experimental values for all nuclei are slightly higher especially for the higher excited states. We believe this is due to the change of the projection of the angular momentum which is due mainly to band crossing.

Unfortunately there is no enough measurements of electromagnetic transition rates $B(E1)$ or $B(E2)$ for these series of nuclei. The only measured $B(E2, 0_1^+ \rightarrow 2_1^+)$'s are presented, in Table 2 for comparison with the calculated values. The parameters $E2SD$ and $E2DD$ are used in the computer code NPBEM [20] for calculating the electromagnetic transition rates after normalization to the available experimental values and displayed in Table 1.

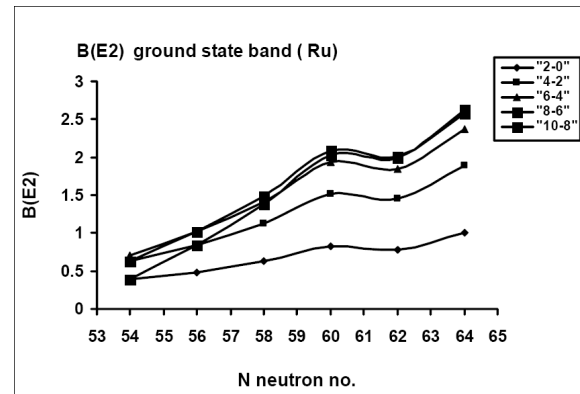
No new parameters are introduced for calculating electromagnetic transition rates $B(E1)$ and $B(E2)$ of intraband and interband. Some of the calculated values are presented in Fig. 3 and show bending at $N = 60, 62$ which means there is an interaction between the $(+ve)$ and $(-ve)$ parity states of the ground state band.

The moment of inertia I and angular frequency $\hbar\omega$ are calculated using equations (11, 12):

$$\frac{2I}{\hbar^2} = \frac{4I - 2}{\Delta E(I \rightarrow I - 2)}, \quad (11)$$

$$(\hbar\omega)^2 = (I^2 - I + 1) \left[\frac{\Delta E(I \rightarrow I - 2)}{(2I - 1)} \right]^2. \quad (12)$$

The plots in Fig. 4 show back bending at angular momentum $I^+ = 10$ for $^{98-108}\text{Ru}$ except ^{106}Ru where there is no experimental data available. It means, there is a crossing between the $(+ve)$ and $(-ve)$ parity states in the ground state band which confirmed by calculating staggering effect to these series of nuclei and the bending observed in Fig. 3.

Fig. 3: The calculated $B(E2)$'s for the ground state band.

3.3 Electric monopole transitions

The electric monopole transitions, $E0$, are normally occurring between two states of the same spin and parity by transferring energy and zero unit of angular momentum. The strength of the electric monopole transition, $X_{if} (E0/E2)$, [27] can be calculated using equations (13, 14) and presented

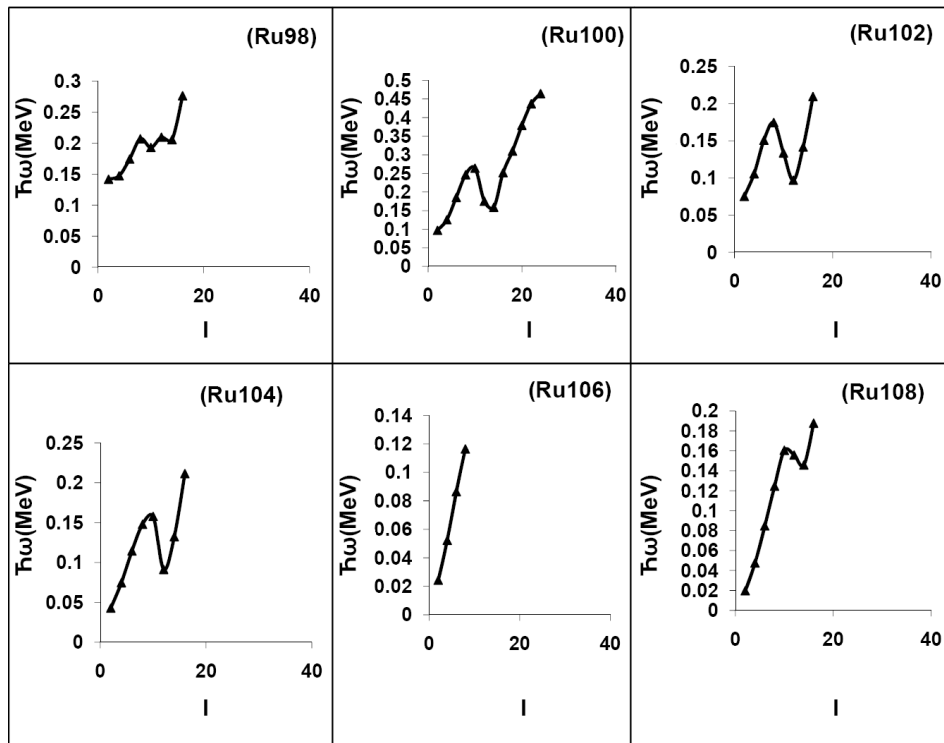


Fig. 4: Angular momentum I as a function of $(\hbar\omega)$.

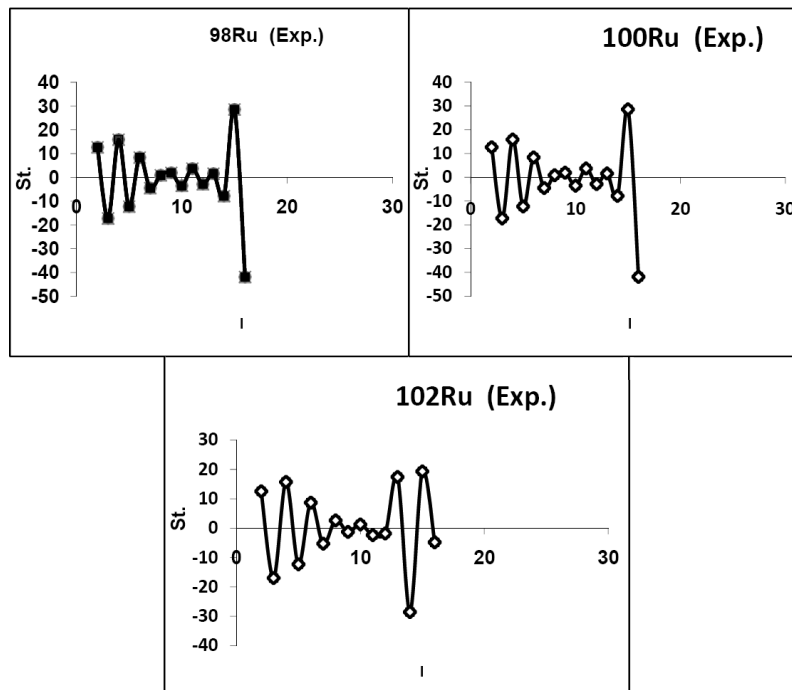


Fig. 5: $\Delta I = 1$, staggering patterns for $^{98-102}\text{Ru}$ isotopes.

in Table 4

$$X_{if'f}(E0/E2) = \frac{B(E0, I_i - I_f)}{B(E2, I_i - I_f)}, \quad (13)$$

$$X_{if'f}(E0/E2) = (2.54 \times 10^9) A^{3/4} \times \frac{E_\gamma^5(\text{MeV})}{\Omega_{KL}} \alpha(E2) \frac{T_e(E0, I_i - I_f)}{T_e(E2, I_i - I_f)}. \quad (14)$$

3.4 The staggering

The presence of $(+ve)$ and $(-ve)$ parity states has encouraged us to study staggering effect [28–30] for $^{98-108}\text{Ru}$ series of isotopes using staggering function equations (15, 16) with the help of the available experimental data [21–26].

$$\text{Stag}(I) = 6\Delta E(I) - 4\Delta E(I-1) - 4\Delta E(I+1) + \Delta E(I+2) + \Delta E(I-2), \quad (15)$$

with

$$\Delta E(I) = E(I+1) - E(I). \quad (16)$$

The calculated staggering patterns are illustrated in Fig. 5 and show an interaction between the $(+ve)$ and $(-ve)$ parity states for the ground state of $^{98-102}\text{Ru}$ nuclei.

3.5 Conclusions

IBA-1 model has been applied successfully to $^{98-108}\text{Ru}$ isotopes and we have got:

1. The levels energy are successfully reproduced;
2. The potential energy surfaces are calculated and show vibrational-like to ^{98}Ru , γ -soft to $^{100-104}\text{Ru}$ and rotational characters to $^{106-108}\text{Ru}$ isotopes where they are mainly prolate deformed nuclei;
3. Electromagnetic transition rates $B(E1)$ and $B(E2)$ are calculated;
4. Bending for $^{98-108}\text{Ru}$ has been observed at angular momentum $I^+ = 10$ except for ^{106}Ru , where there is no experimental data are available;
5. Electromagnetic transition rates $B(E1)$ and $B(E2)$ are calculated;
6. Strength of the electric monopole transitions $X_{if'f}(E0/E2)$ are calculated; and
7. Staggering effect has been calculated and beat patterns are obtained which show an interaction between the $(-ve)$ and $(+ve)$ parity states for $^{98-102}\text{Ru}$.

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